

Error Detection and Correction Using Minimal ParityBased on Matrices

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Abstract—Multiple cell upsets are caused by improvements in complementary metal oxide semiconductor (CMOS) technology (MCUs). MCUs had been a difficult problem for data storage in memory for numerous applications because of the radiation particles. Because of their simple encoding and decoding, error correction codes are one of the approaches that are employed more frequently to safeguard memories. Typically, MCUs have an impact on nearby memory bits. Consequently, a productive strategy would be one that would find and rectify as many neighboring bits as possible. Matrix-based code has only one drawback: it requires a large number of parity bits to facilitate error correction in memories. We reduced the number of parity bits in this document to address the flaw. When compared to other existing strategies, the suggested technique provides an equivalent error-correction capability with a lower parity bit count. Area, power, and delay time have all decreased, along with the total number of parity bits, by 30%, and by 1.12%, 33.59%, and 55.46%, respectively. These factors render the suggested strategy for memory protection effective and efficient. Applications where parity bits and speed are strictly regulated can employ this technique. **Keywords:** Parity bits, Multiple Cells Upset (MCU), ErrorCorrection Codes (ECCs), Matrix Based Codes.

I. INTRODUCTION

Memory is a term used to describe a data storage area. Data in memory is encoded while being stored and decoded when being retrieved. Information can be stored by using distinct storage components and clusteharing them together. Each memory cell has the capacity to hold a single bit of data. The reliability of memory is seriously threatened during data storage by soft mistakes brought on by particle radiation [1][2]. Errors happen when radiation particles come in contact with the system's sensitive parts [3]. The result is a corruption of the data kept in memory. As a result, matrix-based codes are frequently utilized [4][5] to safeguard the data bits in memories. From technique to technique, the bit layout differs. Fig. 1 depicts our method of layout. Some parity bits will also be kept in memory along with the data bits. So, the task of the encoder is to change the p-bit data that is provided into r-bit data, where p-bits are data bits and r-p bits are parity bits. If the ECCs are able to repair the bits in the memory, the decoder takes on the task of doing so and outputs the original data. The complexity of the decoder and encoder circuits as well as the quantity of parity bits determine the overhead of the memory system that is impacted by radiation. For various purposes, different ECCs with overheads and varied correction abilities are chosen.

Based on their demands, such as performance, time, and area complexity. Because they are simple to use, Single Error Correction and Double Error Detection codes (SEC-DED) offer a different approach to correcting ECCs. SEC-DEC codes are unable to fix memory faults brought on by MCUs [4]. MCUs are common as a result of technology scalability. The MCUs appear to target nearby cells whose spacing are shorter than two to three bits, according to recent radiation experiments [6]. Certain types of MCUs, including OLS and DS codes, among others, are handled by ECCs with powerful correction capabilities. They are employed for memory-related purposes. Hence, while choosing ECCs to secure these memories, redundancy overheads or the correction capability are taken into account as key factors. So, in the current work, these aspects are optimized.





Fig. 1. Data Organization in memory

The data acquired from various survey papers has been mentioned in Section II and will be discussed in the following parts. The new matrix-based code and its decoding and encoding procedures are described in Part III. The various cases that the suggested technique can handle and its capacity for rectification are discussed in Section IV. Bitrate, as well asPart V presents the parametric results, and Section VI concludes the discussion.

II. RELATED WORKS

One of the most used strategies in memory applications is matrix-based coding. The single and multiple error detection and correction, as well as the reduction of area, power, and bit overhead, are all goals of the coding schemes.

The combination of parity codes and hamming codes contains more redundant bits, claims the work [7]. These data bits are stored in the encoder as a matrix of order (k x z), and order (11,8,4) diagonal, vertical, and horizontal parity sharing bits are employed to encode the data. Whereas the HVHC (Horizontal Vertical Hamming Code) block corrects errorsthat happened in parity bits, the 3PC (3-Parity Check) block identifies and corrects faults that occurred in data bits. This technique finds and fixes three-bit errors in both parity and data bits. In the paper Adjacent Error Correction using Matrix Based Codes [8], a word is stored in a matrix configuration that is 4 x 8 and includes the extra parity bits generated horizontally and vertically.

In addition to the 32 data bits illustrated in Fig. 2 with this method, there are an additional 8 Hamming bits and 12 vertical parity bits. This technique is typically used for the identification and correction of adjacent 4-bit errors. To eliminate clustering mistakes brought on by MCUs, technique uses up more space and money.

This method allows for the detection and correction of all single bit faults as well as the protection of memories from MCUs and SEUs. With the addition of 8 parity bits and 20 Hamming bits, a 32-bit data set is organized in matrix format of order 4×8 in the work [9]. It can correct any subset of eight faults in a row as long as the other rows have only one bit error, and it can repair one-bit errors as well as numerous errors in a row. The only issue is that when several problems do occur in multiple rows, some of the errors are fixed but others remain corrupted. The 32-bit data is grouped in the [10] approach, 28 parity bits are calculated in the encoder, and 8-bit faults can be fixed using this methodology. Here, a 1-bit error can also be fixed.



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	Data	bits	E H pa	xtende lammir arity bi	ed ng its	Hidde Hamm parity l	en ing bits
D_0	D ₈	D ₁₆	D ₂₄	H_0	r_0	r_1	<i>r</i> ₂
D_1	D 9	D ₁₇	D ₂₅	H_1	r_3	r_4	<i>r</i> ₅
D_2	D ₁₀	D ₁₈	D ₂₆	H_2	<i>r</i> ₆	r 7	<i>r</i> ₈
D_3	D ₁₁	D ₁₉	D ₂₇	H ₃	r 9	<i>r</i> ₁₀	<i>r</i> ₁₁
D_4	D ₁₂	D ₂₀	D ₂₈	H_4	<i>r</i> ₁₂	<i>r</i> ₁₃	<i>r</i> ₁₄
D_5	D ₁₃	D ₂₁	D ₂₉	H_5	<i>r</i> ₁₅	<i>r</i> ₁₆	<i>r</i> ₁₇
D_6	D ₁₄	D ₂₂	D ₃₀	H_6	r ₁₈	<i>r</i> ₁₉	<i>r</i> ₂₀
D ₇	D ₁₅	D ₂₃	D ₃₁	H ₇	<i>r</i> ₂₁	<i>r</i> ₂₂	<i>r</i> ₂₃
					V_0	<i>V</i> ₁	<i>V</i> ₂
					V_3	<i>V</i> ₄	V_5
					V_6	V7	V_8
					V_9	V ₁₀	<i>V</i> ₁₁
					Vertic	al pari	ty bit

Fig. 2. Logic diagram for Low Redundancy Matrix-Based codes for AdjacentError Correction with Parity Sharing

This method's disadvantage is that it cannot fix parity bit issues. Although it is impossible, the parity bits are thought to be error-free. Data bits will be stored in the way described in [11][12] as a matrix of order (8 x 4). In which the extended Hamming coding method is employed toproduce extended parity bits, which are then utilized to detect flaws. The hidden faults are corrected using both hidden bits and regular parity bits. The fundamental flaw in this method is the inability to recognize and correct errors in data bits and associated parity bits that are caused by MCUs.

III. PROPOSED TECHNIQUE

The k-bit data in the proposed technique is organized as a mx n matrix, where the rows and columns are denoted by m and n, respectively (i.e., k = m x n). The data is organized in a matrix row by row, in contrast to the previous work Adjacent Error Correction using Matrix Based Codes. From all the data bits, four Vertical Hamming bits and ten Parity Sharing bits are derived. The bits M8 and M9 in our study are calculated differently using bits that are present in the matrix's DNA (Deoxyribonucleic Acid)-shaped curve, as illustrated in Fig. 3. Also, those portions are split into two parts, which will be discussed further. Consider a 32-bit data set as an example to help clarify our work. The data bits are arranged in a matrix form with m = 8 and n = 4 and are labelled D0 through D31. When the column bits are calculated as shown in equation 1, the extended Hamming parity bits (V0 - V3) are useful for finding faults in the column bits. Equation 1 describes how V0 is computed, as well as how V1 - V3 is determined. Equations 2 to 5 are used to determine how to calculate the horizontal parity sharing bits (M0 to M9). Equation 2 shows how to calculate M2, M4, M6, in the same way that M0 is calculated, and Equation 3 explains how to calculate M3, M5, and M7 in the same manner that M1 is calculated. M8 (shown in Figure 3 as Blue) and M9 (shown in Figure 3 as Yellow) are determined in a special fashion that is reflected in Equations 4 and 5. Equations 1 through 5 contain the Hamming Equation. As a result, the fundamental operation XOR is used to create all of the equations. The overall number of redundant bits calculated has been decreased and the use of imaginary bits has



been eliminated in this technique when compared to previous work on adjacent error correction utilizing matrix- based codes. For extended, syndrome bits are calculated.

D0	D1	D2	<mark>D3</mark>	мо	M1
D4	<mark>D5</mark>	<mark>D6</mark>	D7		
D8	D9	D10	D11	M2	M3
D12	D13	D14	D15		
D16	D17	D18	D19	M4	M5
D20	D21	D22	D23	M6	M7
D24	D25	D26	D27		
D28	D29	<mark>D30</mark>	D31	1/18	M9
V0	V1	V2	V3		

Fig. 3. Logic diagram for Proposed Technique

Bits of hamming parity (V). The parity bit of that particular column will aid in identifying any bits that are affected by errors.

$V0 = D0 \bigoplus D4 \bigoplus D8 \bigoplus D12 \bigoplus D16 \bigoplus D20 \bigoplus D24 \bigoplus D28$	(1)
$M0 = D0 \bigoplus D1 \bigoplus D2 \bigoplus D16 \bigoplus D17 \bigoplus D18$	(2)
M1 = D1 🕀 D3 🕀 D17 🕀 D19	(3)
$M8 = D0 \bigoplus D5 \bigoplus D10 \bigoplus D15 \bigoplus D20 \bigoplus D23 \bigoplus D29 \bigoplus D30$	(4)
$M9=D3\oplusD6\oplusD9\oplusD12\oplusD17\oplusD18\oplusD24\oplusD27$	(5)

Next, the (M0–M9) horizontal parity sharing bits are computed. The corresponding parity bit of that particular row will aid in the detection of any error-affected bits if any are present. The error bit is now fixed. Let's use an illustration to comprehend the procedure. If the fault affects the D1 bit, the syndrome (V0 - V3) will equal 0100, which denotes an error in the second column. Then M0 to M9 horizontal parity sharing bits will aid in identifying that specific row of errors (1st row). Finally, an error-containing bit is found and fixed. It is vital to note that because there are no distinct parity bits for error detection in the parity bits themselves, data bits cannot be identified when there are mistakes in both the parity and data bits that are caused by MCUs. In order to prevent this kind of Parity bits may be spaced apart by an interval more than 3 bits while saving data bits to memory.

These kinds of setups typically prevent parity bit mistakes. On the other side, if there are no errors, additional decoding is omitted, which cuts down on latency. The suggested technique's primary superiority is that it corrects all neighboring horizontal mistakes in rows.



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IV. EVALUATION

When the encoder receives 32-bit data, it outputs 46 bits, which are made up of data bits and parity bits. Then, the decoderreceives these 46 bits as input and checks them for data bit errors. In this section, we discussed many likely MCUs, along with instances of possible memory events and the decoding procedure used to correct the data.

A. One Bit Error

DO	D1	D2	D3	мо	M1
D4	D5	D6	D7		
D8	D9	D10	D11	M2	MЗ
D12	D13	D14	D15		
D16	D17	D18	D19	M4	M5
D20	D21	D22	D23	M6	M7
D24	D25	D26	D27		
D28	D29	D30	D31	M8	M9
V0	V1	V2	V3		

Fig. 4. 1-bit error

For instance, if D0 in Fig. 4 is a damaged bit, errors will appear in M0, V0, and M8. Decoder will therefore recognize D0 bit, and data bit is reversed for restoration.

B. Two Bit Error

DO	D1	D2	D3	мо	M1
D4	D5	D6	D7		
D8	D9	D10	D11	M2	M3
D12	D13	D14	D15		
D16	D17	D18	D19	M4	M5
D20	D21	022	D22		
D20	DZ1	DZZ	DZS	M6	M7
D24	D25	D26	D27		
D28	D29	D30	D31	M8	M9
V0	V1	V2	V3		

Fig. 5. 2-bit error

If D0 and D3 are assumed to be corrupted bits, as shown in Fig. 5, errors will appear in M0, V0, M1, V3, M9, and M8. Decoder will therefore recognize D0 and D3 bits, and data bits are reversed for restoration.

C. Three Bit Error

DO	D1	D2	D3		
D4	D5	D6	D7	мо	M1
D8	D9	D10	D11	M2	M3
D12	D13	D14	D15		
D16	D17	D18	D19	M4	M5
D20	D21	D22	D23	M6	M7
D24	D25	D26	D27		
D28	D29	D30	D31	M8	мэ
VO	V1	V2	V3		
Fig. 6. 3-bit error					



F. Parametric Results

Verilog HDL is used to create both the suggested code and the concealed parity code, which is then simulated in Xilinx Vivado. Using Xilinx ISE, both codes were implemented in Vertex-6. Table II shows that, in comparison to adjacent error correction utilizing matrix-based codes, significantly reduced delay, area, and power have been obtained. The memory's bit storage capacity has been decreased from 52 to 46 bits, and the decoding procedure is carried out without the usage of imaginary bits, as in the work Adjacent Error Correction using Matrix Based codes. According to Table III, consumption of power, area, and delay is decreased by 1.26%, 5.55%, and 21.17%, respectively.

In the event that D0, D1 and D2 are corrupted bits, as in Fig. 6, errors will appear in M0, M1, V0, V1, V2 and M8. Decoder will therefore recognize D0, D1, and D2 bits, and data bits are reversed for restoration.

D. Four Bit Error

DO	D1	D2	D3		
D4	D5	D6	D7	мо	М1
D8	D9	D10	D11	M2	мз
D12	D13	D14	D15		
D16	D17	D18	D19	M4	M5
D20	D21	D22	D23	мө	M7
D24	D25	D26	D27		
D28	D29	D30	D31	M8	M9
VO	VI	V2	V3		
Fig. 7. 4-bit error					

According to Fig. 7, if D0, D1, D2 and D3 are corrupted bits, faults will appear in M0, V0, V1, V2, V3, M9, and M8. As a result, the decoder will recognize the D0, D1, D2, and D3bits and flip the data bits for restoration. The key characteristic of our suggested method, "Adjacent Horizontal Four-Bit

ErrorCorrection," is this.

E. Bit Rate

The Bit Rate is calculated using,

Table II: Comparison of Area, Power and Delay

Codec		Area	Total Power(μW)	Delay(ns)
Matrix	based	72	3.649	2.153
Codec				
Proposed	Codec	68	3.603	1.697

Table III: Percentage Reduction of Area, Power and Delay

Technique	Area %	Power%	Delay %
Encoder	15%	0%	26.96%
Decoder	1.92%	1.95%	57.48%
Proposed Codec	5.55%	1.26%	21.18%

IV. CONCLUSION

The suggested method requires just 14 parity bits and can quickly identify and fix neighboring



problems. Power, area, and latency have all been significantly reduced using this technology. These calculations for Vertex-6 reveal that the power, area, and time delay consumption are lowered by a combined maximum of 1.26%, 5.55%, and 21.17%. The proposed code fits the memory system's rigorous requirements for area and time delay better, according to the results. This approach effectively corrects all single bit errors, a few two- bit errors, and up to four-bit adjacent faults.

In terms of future application, the technique can be extended to fix data bits when there are an even number of column bit mistakes. a method that can fix mistakes even in parity bits.

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